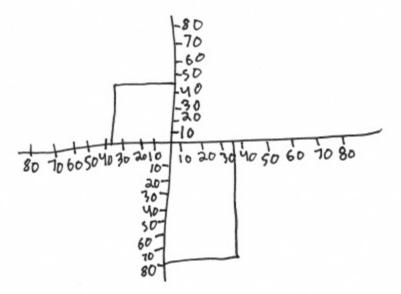
#### **Title: Scary Reunion**

Achievement Level: Novice 1

Criteria and Performance Level	Rationales			
Problem Solving	The student's strategy of constructing a graph to show the location of each shark would work but the student does not correctly plot the points nor calculate the actual distance traveled. The students answers of "a team of marine biologists will need to travel 45 miles per hour to			
Apprentice	be in the same location of shark 1" and "the marine biologists will need to travel 51 miles per hour to see shark 2" are incorrect.			
Reasoning & Proof	The student does not demonstrate understanding of the underlying concepts of finding the distance traveled using a coordinate plane or the Pythagorean Theorem. There is no justification for reasoning			
Novice	present and arguments are made with no mathematical basis.			
Communication	nour and graph. The student makes no attempt to provide a written			
Apprentice	account of their approach for finding 45 miles per hour or 51 miles per hour.			
Connections	The student does not make a mathematical connection about their			
Novice	solution.			
Representation	The student attempts to make a coordinate graph but does not accurately plot the location of shark 1, does not include labels, does			
<i>Apprentice</i> not use it to find the distance or speed traveled.				

Achievement Level: Novice 1

P/S	R/P	Com	Com Con Rep		A/Level			
Α	N A N		N A N A				N	



the teom of Marine Biologists will need to travel 45 miles per hour to be in the Some location of shork 1. The Morine Biolo-gists will need to travel 31 miles on Nour to see Shork 2. That is if they wonted to be in the same location at 7 P.M. because of my Work that I showed above with the graph. Shork I- 45 mph shorls 2.51 mps

#### **Title: Scary Reunion**

Achievement Level: Apprentice 1

Rationales
The student's strategy of using the Pythagorean Theorem works to solve the first part of the task. The student's answer for the first part of
the task is correct, "Shark #2 @ 2 pm = 17 mph" and "Shark #1 @ 2 pm = 15 mph." The student provides no evidence of their strategy that
therefore converting the Shark #1 speed of 15 mph to the boat needing to go 30 mph.
The student demonstrates correct reasoning for some of the underlying concepts of the task, such as using the Pythagorean
Theorem to calculate the distance traveled by each shark at 2 pm, " $36^2$ + $77^2$ = 7225, $\sqrt{7225}$ = 85" and " $45^2$ + $60^2$ = 5625, $\sqrt{5625}$ = 75." The student does not show correct reasoning for calculating the speed of
shark or vessel. The student does not provide mathematical justification for " $85 \div 5 = 17$ mph", " $75 \div 5 = 15$ mph", and "they'll have to go 30 miles per hour."
The student attempts to make an organized and sequenced response, but it is incomplete. The does not communicate their approach including the use of the Pythagorean Theorem, the formula for speed,
or why the boat will have to go 30 mph. The appropriate use of formal math language is minimal including <i>fast, mph, slower, miles per hour</i> .
The student's connection is contextually irrelevant, "Shark One is slower so it will be easier to catch" as it does not explore the concept

Representation	The student attempts to construct a coordinate grid to investigate the location of the shark after 5 hours. The student does not provide any
Apprentice	labels for the data provided on the grid or for the units on the x and y coordinates.

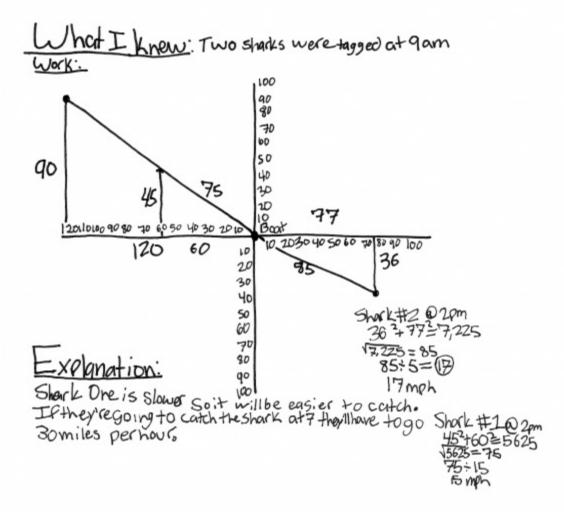
#### Note:

The overall achievement level for this piece of student work falls under Exemplars exception to the rule category. If a student has all Apprentice scores or above, but a Novice in "Connections," the student may still receive an achievement level score of Apprentice. To learn more about Exemplars scoring, please refer to the section of your dashboard called "Tools for Success" and click on the link for "Using the Assessment Rubric."

Achievement Level: Apprentice 1

P/S	R/P	Com	m Con Rep		A/Level
Α	Α	Α	Ν	Α	Α

Scary Reunion Question Statement: How fast does the teamneed to inorder to catch up to the shorks?



#### **Title: Scary Reunion**

Achievement Level: Apprentice 2

Criteria and Performance Level	Rationales
Problem Solving <i>Apprentice</i>	The student makes mistakes in determining how far the sharks traveled. The student correctly uses the Pythagorean Theorem for incorrect values of the distances traveled by each shark. The student correctly uses the formula for speed but arrives at an incorrect answer due to their previous mistake. The student incorrectly states "The boat would have to go 17.1 or 17 mph to be near shark 1 at 7 pm" and "The boat would have to go 19.3 or 19 mph to be near shark 2 at 7 pm."
Reasoning & Proof <i>Practitioner</i>	The student demonstrates correct reasoning of the Pythagorean Theorem, " $45^2 + 165^2 = c^{2"}$ and " $36^2 + 190^2 = c^{2"}$ . The student correctly uses the formula for speed, "speed = distance $\div$ time" to provide mathematical justification for the speed of the sharks, " $171 \div 10 = 17.1$ mph", and " $193 \div 10 = 19.3$ mph."
Communication <i>Apprentice</i>	The student attempts to construct an organized, sequenced and labeled response but is inconsistent on defining each step of their approach. The student does not explain why they used "60 + 45 = 105" and "36 + 77 = 113" to determine how far each shark traveled in the first five hours.
Connections Apprentice	The student attempts to make a mathematically relevant connection, "I realized that I need to find the hypotenuse first." This connection is relevant but does not explore or clarify how this would change their approach or final answer.

# Exemplars -

Depresentation	The student constructs multiple diagrams to help them solve the
Representation	problem and to portray their thinking. The diagrams appropriately and
Practitioner	accurately represent the student's approach that illustrates where
	mathematical misconceptions occurred.

### Exemplars -

Achievement Level: Apprentice 2

		P/S	R/P	Com	Con	Rep	A/Level
		Α	Р	Α	Α	Ρ	Α
S	cary Benion						
The question is asking me how for if they wanted to be in the sam	st a research Vessei e Place as a Shark gum	Wark by	7 p	ne to m.		Ð	
Sharth 2: 45 miles	Shark 2: Jamiles Jem				Spee	uthouser	
60+45= 105-> Shark troveled 105 miles	36+77= 113-7 Shark trave	6113	miles		ed Zd	*	
A Sharks continue at the same	speed and same di		ont		Speed distance; time	the room adulation	
50+105=165	Shark 2: 26mile - 77+113=190	· · ·	7		me		
453+1652= c2 02=45	36-+ 190= c2	0 mile 0=36 6=19	5				
129220=JCa c=?	1:396+36100=c2	c=?					
C≈171 ?≈171 Shark 1: 171 miles NW	C≈193 Shark2: 193	?≈10	13 IS SE				
distance time (17.1 mph) IO hours	distance time 193=10=(19.3 mph)	1 10	hours	\$			
The boat would have to go 17.1 or 17 mph to be hear sharks at 7 pm.	The boat would have 19 MPh to be near 2 pm	ve te ar s	go nark		or	Z	
	o find the hypo	tenu	se .	fiist	this		

I realized that I need to is rough draft/fist draft. mot, This 4,00 The Naboteunase

#### **Title: Scary Reunion**

Criteria and Performance Level	Rationales
Problem Solving Practitioner	The student's strategy of plotting the position of each shark on a coordinate grid and using the Pythagorean Theorem to calculate the distance traveled in the first 5 hours works to solve the task. The student's answer of the boat needing to travel 30 mph to catch shark 1 and 34 mph to catch shark 2 is correct.
Reasoning & Proof <i>Practitioner</i>	The student shows understanding that the Pythagorean Theorem can be used to calculate the distance each shark traveled, " $45^2 + 60^2 =$ 5,625 = c <sup>2</sup> , c = 75 miles." The student correctly calculates the speed of each shark, "75 ÷ 5 = 15 mph" and "85 ÷ 5 hrs = 17 mph" and then determines the speed of the boat "which is double the distance at 2 pm."
Communication Practitioner	The student correctly identifies the problem to be solved in their opening statement, describes their approach in an organized and coherent response, and states a correct conclusion. Appropriate formal math language such as <i>Pythagorean Theorem, mph, distance,</i> <i>graph, double, constant rate</i> is used to share and clarify ideas.
Connections Practitioner	The student makes a mathematically relevant connection by exploring the concept of a "constant rate of 15 mph". The student uses this connection to determine to double the speed of the boat to catch the shark in 5 hours.

# Exemplars -

	The student's coordinate grid is appropriate and accurate for
	determining the location of the shark after 5 hours and after 10 hours.
Representation	The student uses the coordinate grid to analyze the relationship
Expert	between the distance traveled in the first 5 hours and in the second
LAPER	five hours. All necessary labels are provided and the entered data is
	correct.

	P/S	R/P	Com	Con	Rep	A/Level
	Ρ	Р	Р	Р	Е	Р
Scary Reunion						
How fast would the research vessel , to be in a location near one of the shark	leed S by	to 7 P	trave M?	ι		
Shark 1: 45 miles north, 60 miles west to Shark 2: 36 miles South, 77 miles east After smarth 90.	fter 5 ha	5 na US	urs h	N+E S	E	
1pm 80 70						
90mi 2 pm shark 1 50 45mi 75mi 30						
120110 100 90 80 70 60 50 90 30 20 10 × 77m:	90 100	10 00	BO 140	159160	~	
120mi 60mi 10 20 30 We use pythagdrean theorean 40 85mi	36m Shari	12				
to find the distance troveled so Shark 1 at + b2 = c2 60 Shark 2 452 + 62 = E (25 70	2R			1		
$\sqrt{5,625} = 75$ miles $\sqrt{7,225} =$	85.			7pv	4	
75-5=(15) speed of shark $1=(15 \text{ mph})$ speed of		(2	1			
We divide by s bc this is the location of the shark after shows	Ph	)				
(speed is distance (miles)) divided by time (nours)						

Shark 1 is Slower so we are going to catch that one.

When the boat leaves, the shark is going 15mph and is located 45 miles north and 60 miles west. According to the graph Shark1 is boated at (120,90) which is double the distance at 2 pm. Because Shark 1 is going at a constant rate of 15 mpth, if the boat leaves at 2pm going 30 MPH it will meet the Shark at EXACTLY 7 pm.

If they were to catch Shark 2 they would have to travel 34 MPH to meet the shark at 7pm. I know this because Shark 2 travels 17 MPH. If the boat wants to meet Shark 2 at exactly 7pm they would have to travel at 34 MPH exactly.

Shark 1 Boot Speed: 30MPH Boot Speed: 34 MPH

To most exactly at 7PM

#### **Title: Scary Reunion**

Criteria and Performance Level	Rationales
Problem Solving <i>Practitioner</i>	The student's strategy of drawing diagrams to show the shark's journey, using the Pythagorean Theorem to calculate the sharks' distance traveled in 5 hours, and the formula for speed effectively solves the task. The student's answer of needing to travel 30 mph to be near shark 1 and to go 34 mph to be near shark 2 is correct.
Reasoning & Proof <i>Practitioner</i>	The student correctly applies the Pythagorean Theorem to calculate the distance traveled by each shark, " $60^2 + 45^2 = c^2$ , c = 75 miles" and " $36^2 + 77^2 = c^2$ , c = 85 miles". The student recognized that they needed to "double(d) their distance" to determine the total distance traveled by the boat. The student also correctly uses the formula for finding "speed = distance $\div$ time" to correctly find how fast the boat needs to travel in 5 hours.
Communication Practitioner	The student correctly identifies the problem, describes the steps to the solution, and states a correct conclusion in the last paragraph. Appropriate formal math language such as <i>Pythagorean Theorem,</i> <i>speed, distance, time, hypotenuse, right triangles, 90</i> • <i>turns, formula, doubled, mph</i> are used to share and clarify ideas.

Connections Practitioner	The student notes the regularity that "they swam that distance in 5 hours (9 am - 2 pm), but they actually had 10 hours (9 am - 7 pm) to swim so I doubled their distance." The student makes an important observation that sharks "wouldn't make 90 ° turns, so I found the hypotenuse, a more realistic path." The student makes a connection with what they understand in the real world about swimming behavior.
Representation Practitioner	The student uses a diagram to show the distances and directions the sharks traveled. The diagrams are labeled correctly and show that the distance traveled by the shark is likely the hypotenuse between 2 points.

Achievement Level: Practitioner 2

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	P/S	R/P	Com	Con	Rep	A/Level
방법에 있는 것은 것을 알려야 한 것이 좋다. 말 것은 것을 받는 것을 했다.	Р	Р	Р	Р	Ρ	Р
The question is asking me how fast a researce to go to be near a shark at 7 pm. I will Shark 1: 2pm 60 miles I Shark 2: 9am to a=60 b=45 c=? ?=75 60 2445 2=c2 3600 2005=c2 I Date Ment 75 miles in 5 I Shark 2 Went hours. That means it went 150 miles I That means it	to the second se	2pm	e would agort ine de :: : b c ? : niles	d ha ean he 36 77 85	ve theo dista	
in 10 hours. Speed = 150:5 Speed = <u>150:5</u> Speed = <u>170:5</u> Speed = <u>17</u>	5 mph 1 ha n mber . would	ear found	to g shar f thi mak	ngst of		

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#### **Title: Scary Reunion**

Criteria and Performance Level	Rationales
Problem Solving Practitioner	The student's strategy of using a coordinate grid helps them recognize they need "to find the diagonal distance for each shark." The student uses the Pythagorean Theorem to calculate the diagonal distance of each shark at 2 pm, the formula for speed = $\frac{\text{Distance}}{\text{Time}}$ to calculate the shark's speed, and then "you double the sharks speed because the vessel goes the same distance at half the time." The students answer that "for shark #1 the vessel must go 30 mph whist the vessel would have to go 34 mph to reach shark #2" is correct.
Reasoning & Proof <i>Practitioner</i>	The student's arguments are constructed with adequate mathematical basis. The student correctly applies the Pythagorean Theorem to calculate the distance traveled by each shark, " $60^2 + 45^2 = c^2$ , $c = 75$ miles" and " $36^2 + 77^2 = c^2$ , $c = 85$ miles." The student correctly justifies the speed of each shark, " $75$ miles $\div 5$ hours = 15 mph, 85 miles $\div 5$ hours = 17 mph." The student also shows correct reasoning for how fast the boat would need to travel by doubling the shark's speed over 5 hours to catch up with the shark in 10 hours.

Communication Practitioner	A sense of purpose is communicated by the student in the original Question section, "If they wanted to pull up the anchor a 2 pm and end up near one of the sharks, how fast would the vessel have to average?" The student's approach is provided within the Explanation, "First I had to find the Diagonal distance for each shark" and "I then used the formula for speed = D/T to find each SHARKS speed." Appropriate formal math language such as <i>average</i> , <i>location</i> , <i>speed</i> , <i>distance</i> , <i>time</i> , <i>"diagonal distance"</i> , <i>"pathgarum therum"</i> , <i>right triangle</i> , <i>formula</i> , <i>double</i> ,
Connections	<i>mph</i> are used to share and clarify ideas. The student solves the tasks and notes the pattern "the sharks distance forms a right triangle." The student explores the relationship "the vessel needs to travel double the speed the sharks go."
	The student's use of a coordinate grid and compass rose to illustrate the position of each shark after 5 hours is appropriate and accurate. All necessary labels are provided and the information is correct.

	P/S	R/P	Com	Con	Rep	A/Level
	Р	Ρ	Р	Р	P	Р
Scary Reunion						
Question If they wanted to pull up the anchor at 2 pm end up near one of the sharks, how fast the vessel have to average?	and Woul	6	Ak -	K	E.	
Information needed Shark locations - shork I · 45 miles N & 60 miles W - Shark 2						
• 36 miles S & 77 miles E • tagged at 9 am • Pulled anchor @ 2pm • Meets one of the sharks @ 7pm • All 5 hour difference 36	. 85	Shrs	miles			
· Speed = <u>Distance</u> · A <sup>2</sup> + B <sup>2</sup> = C <sup>2</sup> (Pythogorean theorem)	44		ows.	·		
C=The Diagonal Distance the shark travels Shark #1 Shark # 2				/		
$60^{2} + 45^{2} = c^{2}$ $3600 + 2025 = C^{2}$ 3600 + 2025 = 5625 3600 + 2025 = 5625 3600 + 2025 = 5625 $3225 = 40^{2}$ C = 85miles Answer, Fo	- 5 00	- b	मन		-	
C = 75 miles I noticed that you could use the vessel is the pythagorean theory because the vessel is the shorks' Distance forms whilst the v	essel	90	30 10 h			
#1 75 miles: 5 hours = 15 mph speed of shark shark #2 #2 85 miles: 5 hours = 17 mph speed of shark		r eau	-n		1	
15+15=30 Explanation: 17+17=34 First 1 had to find the Diagonal Shark. Then 1 used the known because 9am -2pm are 5 hrs a part. 1 then used the	fact	that	the	time	S	
is 5 hrs and that's Speed = D/T to find each Shark' how long the Sharks the boot starts late, and the sh traveled for the distance, the vessel needs	s spo arks to to	go go	doub	le ble		
you double the sharks the speed the sharks go. T speed because the vessel goes the some distance in half the time The speed the vessel needs	ph (Sh	or K. Z	J. T	his i	2	

#### **Title: Scary Reunion**

Achievement Level: Expert 1

Criteria and Performance Level	Rationales
Problem Solving <i>Expert</i>	The student's strategy of drawing a diagram using the provided directional information works to find the distance traveled by the sharks in 5 hours and 10 hours. The student uses their diagram to show that there would be two congruent triangles creating a doubling of the distance traveled. The student's alternate strategy uses the Pythagorean Theorem to calculate the distance the shark traveled in the first 5 hours and then doubling it to find its distance at 7 pm. The student's answer of the boat needing to travel 30 mph to catch shark 1 and 34 mph to catch shark 2 is correct. The student recognizes that the shark is likely to travel twice the distance in twice the time to determine how far the shark will have traveled by 7 pm.
Reasoning & Proof <i>Expert</i>	The student demonstrates correct reasoning by using Pythagorean theorem to find distance traveled on a coordinate grid, $a^{2+} b^{2} = c^{2}$ . The student also uses the speed formula to find the correct speed the boat will need to travel to catch both sharks in 5 hours, "Shark 1: $\frac{150}{5} = 30$ , 30 miles per hour to catch the shark" and "Shark 2: $\frac{170}{5} = 34$ , 34 miles per hours to catch the shark. The student utilizes their diagram as evidence to support their conclusion of the distance traveled by the shark at 5 hours and 10 hours.

Communication <i>Expert</i>	The student uses a methodical, organized and sequenced response to communicate their approach. The student correctly identifies the problem, describes the steps to the solution, and states a correct conclusion. Insight is communicated about an efficient strategy when the student states "The sharks will double their distance by 7 pm." The student utilizes their insight to construct the congruent triangles and to move from "x = 75 miles" to "2x = 150 miles" to find the total distance needed to travel. Appropriate math language, such as <i>diagram, location, difference, double, distance, Pythagorean Theorem, hypotenuse, miles, time, miles per hour, speed</i> is used rigorously to share and clarify ideas.
Connections <i>Expert</i>	The student uses several alternative strategies for finding the distance traveled and the speed required to make a mathematically relevant math connection. The student explains the phenomena that "the boat has to travel at double the speed of the sharks, because it travels double the distance in the same amount of time."
Representation <i>Expert</i>	The student analyzes the relationships between the distance the sharks travel in 5 hours and 10 hours by using congruent triangles to show the total distance traveled. The student uses the diagram to clarify that doubling the time doubles the distance traveled.

Achievement Level: Expert 1

		_				
	P/S	R/P	Com	Con	Rep	A/Level
	E	Е	E	Е	E	E
Scary Reunion						
A team of marine biologists are studying sha the team's research vessel need to travel in or by 7:00 pm if they leave at 2:00 pm? I amgoing to make a diagram, as this will help shark locations and come up with a solution.					irK	
Strategy 1: 120mi From 9:00 am a 5 hour difference Th 150mi X=T5mi X=T5mi Hour difference Th their distant x: distant	fference. there is he Shark. he by T. ht. to shar	swind the	n Z: 5 hou jill d pm.	oop ,r	m	
Using Pythagorean theorem $X^2$ : dis to find the hypotenuse $36 \text{ mil}$ $Y: 85 \text{ mi}$ $a^2 + b^2 = c^2$ $45^2 + 60^2 = x^2$ $12 \text{ mi}$ $Y = 77 \text{ mi}$ $x^2 = 5,625$ $x = 75 \text{ mi} x^2 = 150 \text{ miks}$ (Dist at 7:00 pm	36mi	_!	70 mi	11		
$36^{2} \cdot 77^{2} = \chi^{2}$ $\chi^{2} = 7.225$ $\chi = 85m_{1}2\chi = 1.70$ miles Dist at 7:00 pm	15 4mi				ine	
To find the necessary speed, I need to divide distant	nce (150 mi	110	M1) E	y T	Ime	

(5 hours)

Shark 1:  $\frac{150}{5} = 30$  30 miles per hour to catch the shark

Shark Z: 170 = 34 34 miles per hour to catch the shark.

Speed of Shark 1= 75 = 15 mph	The boat has to travel at
15.2=30 Boat travels 30 mph	double the speed of the
Speed of Shark Z=8515=17 mph	sharks, because it travels
17.2=34 Boat travels 34 mph	double the distance in the
11.2=39 Boar francis s to pr	same amount of time

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#### Scary Reunion Explanation

I started solving this problem by making a diagram that represents the location of the sharks in relation to the research boat. Shark 1 was 45 miles north and 60 miles west, and Shark 2 was 36 miles south and 77 miles east. Because the shark's travel pattern creates a right triangle, I was able to use the Pythagorean theorem to find the hypotenuses of the two triangles. Shark 1 was 75 miles away and shark 2 was 85 miles away. At 9:00 am, the sharks were released and traveled their respective distances by 2:00 pm (a 5 hour difference). By 7:00pm (when the researchers have to catch the shark by), the sharks will have doubled their distance so the researchers have to travel 150 miles for shark I and 170 miles for shark z (bothin 5 hours). Dividing distance by time, I get the necessary speed for shark I to be 30 miles per hour and the necessary speed for shark Z to be 34 miles per hour. Another way I did it was to compare the speed of the sharks to the boat speed. Shark | travels 75 miles in 5 hours, so its speed is 15 mph. The boat has to be double that because it travels double the distance in the same time. The refore, the necessary speed for the boat for shark I again turns out to be 30 mph. For shark 2, Its speed is IT mon (85/5), so the boats speed has to be 34 mph.